INTRODUCTION

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Contents

1. Overview

0001 Besides the book by Laumon and Moret-Bailly, see [LMB00], and the work (in progress) by Fulton et al, we think there is a place for an open source textbook on algebraic stacks and the algebraic geometry that is needed to define them. The Stacks Project attempts to do this by building the foundations starting with commutative algebra and proceeding via the theory of schemes and algebraic spaces to a comprehensive foundation for the theory of algebraic stacks.

We expect this material to be read online as a key feature are the hyperlinks giving quick access to internal references spread over many different pages. If you use an embedded pdf or dvi viewer in your browser, the cross file links should work.

This project is a collaborative effort and we encourage you to help out. Please email any typos or errors you find while reading or any suggestions, additional material, or examples you have to stacks.project@gmail.com. You can download a tarball containing all source files, extract, run make, and use a dvi or pdf viewer locally. Please feel free to edit the LaTeX files and email your improvements.

2. Attribution

06LB The scope of this work is such that it is a daunting task to attribute correctly and succinctly all of those mathematicians whose work has led to the development of the theory we try to explain here. We hope eventually to generate enough community interest to find contributors willing to write sections with historical remarks for each and every chapter.

Those who contributed to this work are listed on the title page of the book version of this work and online. Here we would like to name a selection of major contributions:

(1) Jarod Alper contributed a chapter discussing the literature on algebraic stacks, see Guide to Literature, Section 1.
(2) Bhargav Bhatt wrote the initial version of a chapter on étale morphisms of schemes, see Étale Morphisms, Section 1.
(3) Bhargav Bhatt wrote the initial version of More on Algebra, Section 80.
(4) Kiran Kedlaya contributed the initial writeup of Descent, Section 4.
(5) The initial versions of
    (a) Algebra, Section 27,
    (b) Injectives, Section 2, and
    (c) the chapter on fields, see Fields, Section 1.

    are from The CRing Project, courtesy of Akhil Mathew et al.
(6) Alex Perry wrote the material on projective modules, Mittag-Leffler modules, including the proof of Algebra, Theorem 94.5.
(7) Alex Perry wrote the chapter on deformation theory a la Schlessinger and Rim, see Formal Deformation Theory, Section 1.
(8) Thibaut Pugin, Zachary Maddock and Min Lee took notes for a course which formed the basis for a chapter on étale cohomology, see Étale Cohomology, Section 1.
(9) David Rydh has contributed many helpful comments, pointed out several mistakes, helped out in an essential way with the material on residual gerbes, and was the originator for the material in More on Groupoids in Spaces, Sections 12 and 15.
(10) Burt Totaro contributed Examples, Sections 57, 58, and Properties of Stacks, Section 12.
(11) The chapter on pro-étale cohomology, see Pro-étale Cohomology, Section 1, is taken from a paper by Bhargav Bhatt and Peter Scholze.
(12) Bhargav Bhatt contributed Examples, Sections 64 and 68.
(13) Ofer Gabber found mistakes, contributed corrections and he contributed Varieties, Lemma 7.17, Formal Spaces, Lemma 9.5, the material in More on Groupoids, Section 15, the main result of Properties of Spaces, Section 17, and the proof of More on Flatness, Proposition 25.13.
(14) János Kollár contributed Algebra, Lemma 118.2 and Local Cohomology, Proposition 7.7.
(15) Kiran Kedlaya wrote the initial version of More on Algebra, Section 81.
(16) Matthew Emerton, Toby Gee, and Brandon Levin contributed some results on thickenings, in particular More on Morphisms of Stacks, Lemmas 3.7, 3.8, and 3.9.
(17) Lena Min Ji wrote the initial version of More on Algebra, Section 105.
(18) Matthew Emerton and Toby Gee wrote the initial versions of Geometry of Stacks, Sections 3 and 5.

3. Other chapters

Preliminaries

(1) Introduction
(2) Conventions
(3) Set Theory
(4) Categories
(5) Topology

References

[LMB00] Gérard Laumon and Laurent Moret-Bailly, *Champs algébriques*, Ergebnisse der Mathematik und ihrer Grenzgebiete. 3. Folge., vol. 39, Springer-Verlag, 2000.